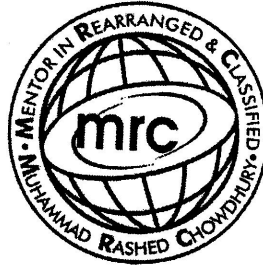


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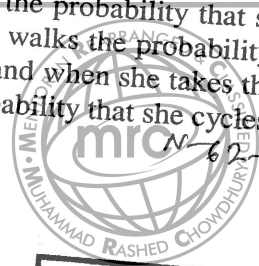
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# Probability & Statistics 1

## TOPIC- Probability

# Probability

- 1 When Anya goes to school, the probability that she walks is 0.3 and the probability that she cycles is 0.65; if she does not walk or cycle she takes the bus. When Anya walks the probability that she is late is 0.15. When she cycles the probability that she is late is 0.1 and when she takes the bus the probability that she is late is 0.6. Given that Anya is late, find the probability that she cycles. [5]



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# Probability

- 2 Maria has 3 pre-set stations on her radio. When she switches her radio on, there is a probability of 0.3 that it will be set to station 1, a probability of 0.45 that it will be set to station 2 and a probability of 0.25 that it will be set to station 3. On station 1 the probability that the presenter is male is 0.1, on station 2 the probability that the presenter is male is 0.85 and on station 3 the probability that the presenter is male is  $p$ . When Maria switches on the radio, the probability that it is set to station 3 and the presenter is male is 0.075.

(i) Show that the value of  $p$  is 0.3.

(ii) Given that Maria switches on and hears a male presenter, find the probability that the radio was set to station 2.

[1]

[4]

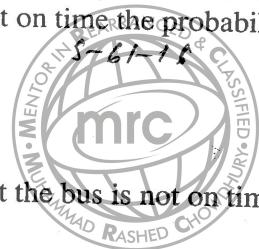


# Probability

3 The probability that the school bus is on time on any particular day is 0.6. If the bus is on time the probability that Sam the driver gets a cup of coffee is 0.9. If the bus is not on time the probability that Sam gets a cup of coffee is 0.3.

(i) Find the probability that Sam gets a cup of coffee. [2]

(ii) Given that Sam does not get a cup of coffee, find the probability that the bus is not on time. [3]



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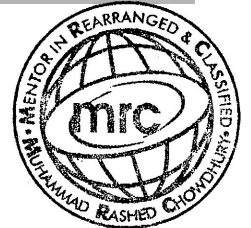
# Probability

4 Three identical cans of cola, 2 identical cans of green tea and 2 identical cans of orange juice are arranged in a row. Calculate the number of arrangements if

- (i) the first and last cans in the row are the same type of drink, [3] P
- (ii) the 3 cans of cola are all next to each other and the 2 cans of green tea are not next to each other. [5]



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# Probability

- 5 The heights of books in a library, in cm, have a normal distribution with mean 21.7 and standard deviation 6.5. A book with a height of more than 29 cm is classified as 'large'. 5-3-15 P
- (i) Find the probability that, of 8 books chosen at random, fewer than 2 books are classified as large. [6]
- (ii)  $n$  books are chosen at random. The probability of there being at least 1 large book is more than 0.98. Find the least possible value of  $n$ . [3]

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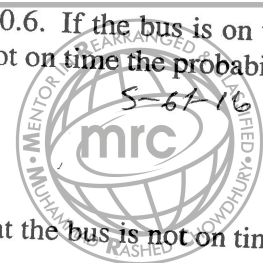


# Probability

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(i) Find the probability that Sam gets a cup of coffee.

(ii) Given that Sam does not get a cup of coffee, find the probability that the bus is not on time.



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# Probability

- 7 Bag A contains 4 balls numbered 2, 4, 5, 8. Bag B contains 5 balls numbered 1, 3, 6, 8, 8. Bag C contains 7 balls numbered 2, 7, 8, 8, 8, 8, 9. One ball is selected at random from each bag. *N-61-11*
- (i) Find the probability that exactly two of the selected balls have the same number. [5]
- (ii) Given that exactly two of the selected balls have the same number, find the probability that they are both numbered 2. [2]
- (iii) Event  $X$  is 'exactly two of the selected balls have the same number'. Event  $Y$  is 'the ball selected from bag A has number 2'. Showing your working, determine whether events  $X$  and  $Y$  are independent or not. [2]





# Probability

2 A fair triangular spinner has three sides numbered 1, 2, 3. When the spinner is spun, the score is the number of the side on which it lands. The spinner is spun four times.

- (i) Find the probability that at least two of the scores are 3.
- (ii) Find the probability that the sum of the four scores is 5.



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[3]

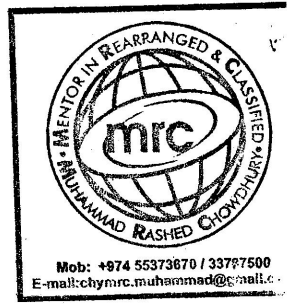
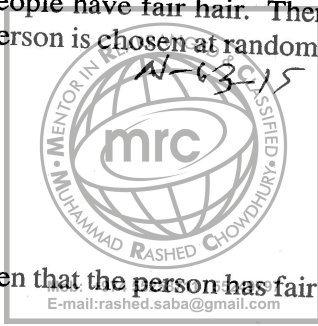
[3]



# Probability

2 In country  $X$ , 25% of people have fair hair. In country  $Y$ , 60% of people have fair hair. There are 20 million people in country  $X$  and 8 million people in country  $Y$ . A person is chosen at random from these 28 million people.

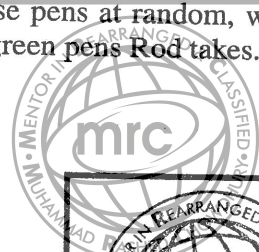
- (i) Find the probability that the person chosen is from country  $X$ . [1]
- (ii) Find the probability that the person chosen has fair hair. [2]
- (iii) Find the probability that the person chosen is from country  $X$ , given that the person has fair hair. [2]



# Probability

- 1 Ashok has 3 green pens and 7 red pens. His friend Rod takes 3 of these pens at random, without replacement. Draw up a probability distribution table for the number of green pens Rod takes. [4]

N- 61-12



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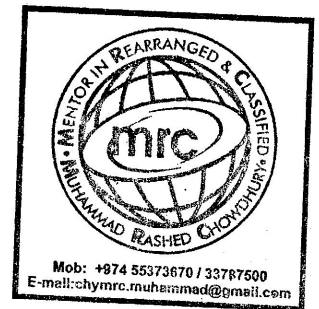
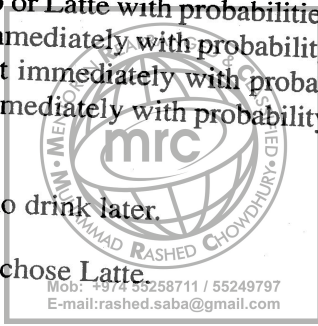


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# Probability

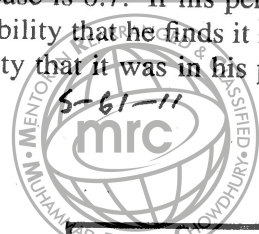
1 Fabio drinks coffee each morning. He chooses Americano, Cappucino or Latte with probabilities 0.5, 0.3 and 0.2 respectively. If he chooses Americano he either drinks it immediately with probability 0.8, or leaves it to drink later. If he chooses Cappucino he either drinks it immediately with probability 0.6, or leaves it to drink later. If he chooses Latte he either drinks it immediately with probability 0.1, or leaves it to drink later.

- (i) Find the probability that Fabio chooses Americano and leaves it to drink later. [1]
- (ii) Fabio drinks his coffee immediately. Find the probability that he chose Latte. [4]



# Probability

- 2 When Ted is looking for his pen, the probability that it is in his pencil case is 0.7. If his pen is in his pencil case he always finds it. If his pen is somewhere else, the probability that he finds it is 0.2. Given that Ted finds his pen when he is looking for it, find the probability that it was in his pencil case. [4]



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# Probability

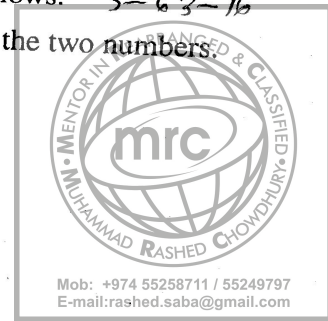
3 Two ordinary fair dice are thrown. The resulting score is found as follows.

- If the two dice show different numbers, the score is the smaller of the two numbers.
- If the two dice show equal numbers, the score is 0.

- (i) Draw up the probability distribution table for the score.
- (ii) Calculate the expected score.

5-6-3-16

P



[4]

[2]



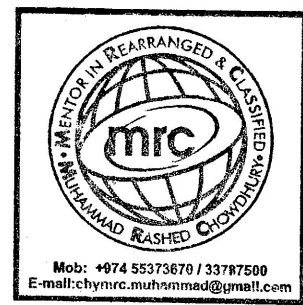
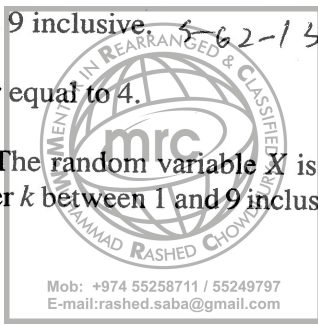


# Probability

- 4 Robert uses his calculator to generate 5 random integers between 1 and 9 inclusive. <sup>5-62-13</sup>
- (i) Find the probability that at least 2 of the 5 integers are less than or equal to 4. [3]

Robert now generates  $n$  random integers between 1 and 9 inclusive. The random variable  $X$  is the number of these  $n$  integers which are less than or equal to a certain integer  $k$  between 1 and 9 inclusive. It is given that the mean of  $X$  is 96 and the variance of  $X$  is 32.

- (ii) Find the values of  $n$  and  $k$ . [4]



# Probability

- 5 (a) John plays two games of squash. The probability that he wins his first game is 0.3. If he wins his first game, the probability that he wins his second game is 0.6. If he loses his first game, the probability that he wins his second game is 0.15. Given that he wins his second game, find the probability that he won his first game. [4]
- (b) Jack has a pack of 15 cards. 10 cards have a picture of a robot on them and 5 cards have a picture of an aeroplane on them. Emma has a pack of cards. 7 cards have a picture of a robot on them and  $x - 3$  cards have a picture of an aeroplane on them. One card is taken at random from Jack's pack and one card is taken at random from Emma's pack. The probability that both cards have pictures of robots on them is  $\frac{7}{18}$ . Write down an equation in terms of  $x$  and hence find the value of  $x$ . [4]



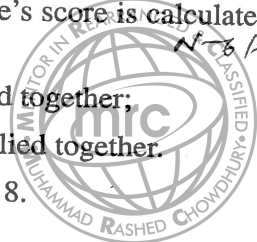
# Probability

3 Jodie tosses a biased coin and throws two fair tetrahedral dice. The probability that the coin shows a head is  $\frac{1}{3}$ . Each of the dice has four faces, numbered 1, 2, 3 and 4. Jodie's score is calculated from the numbers on the faces that the dice land on, as follows:

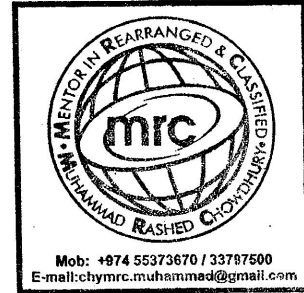
- if the coin shows a head, the two numbers from the dice are added together;
- if the coin shows a tail, the two numbers from the dice are multiplied together.

Find the probability that the coin shows a head given that Jodie's score is 8.

[5]



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# Probability

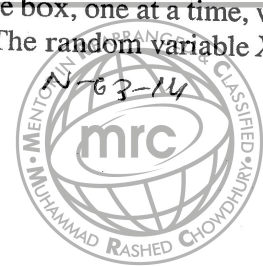
- 7 A box contains 2 green apples and 2 red apples. Apples are taken from the box, one at a time, without replacement. When both red apples have been taken, the process stops. The random variable  $X$  is the number of apples which have been taken when the process stops.

(i) Show that  $P(X = 3) = \frac{1}{3}$ .

- (ii) Draw up the probability distribution table for  $X$ .

Another box contains 2 yellow peppers and 5 orange peppers. Three peppers are taken at random from the box without replacement.

- (iii) Given that at least 2 of the peppers taken from the box are orange, find the probability that all 3 peppers are orange.



[3]

[3]

P



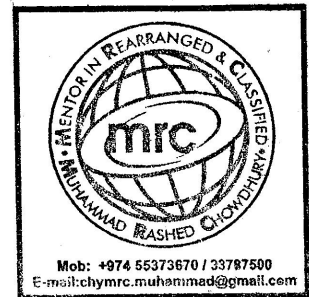
# Probability

5 Three friends, Rick, Brenda and Ali, go to a football match but forget to say which entrance to the ground they will meet at. There are four entrances,  $A$ ,  $B$ ,  $C$  and  $D$ . Each friend chooses an entrance independently.

- The probability that Rick chooses entrance  $A$  is  $\frac{1}{3}$ . The probabilities that he chooses entrances  $B$ ,  $C$  or  $D$  are all equal.
- Brenda is equally likely to choose any of the four entrances.
- The probability that Ali chooses entrance  $C$  is  $\frac{2}{7}$  and the probability that he chooses entrance  $D$  is  $\frac{3}{5}$ . The probabilities that he chooses the other two entrances are equal.

(i) Find the probability that at least 2 friends will choose entrance  $B$ . [4]

(ii) Find the probability that the three friends will all choose the same entrance. [4]



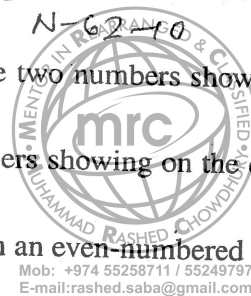


# Probability

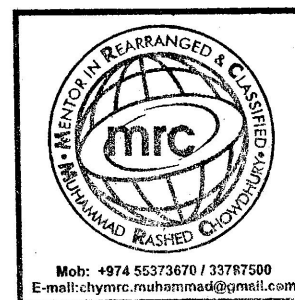
3 A fair five-sided spinner has sides numbered 1, 2, 3, 4, 5. Raj spins the spinner and throws two fair dice. He calculates his score as follows.

- If the spinner lands on an **even-numbered** side, Raj **multiplies** the two numbers showing on the dice to get his score.
- If the spinner lands on an **odd-numbered** side, Raj **adds** the numbers showing on the dice to get his score.

Given that Raj's score is 12, find the probability that the spinner landed on an even-numbered side.



[6]



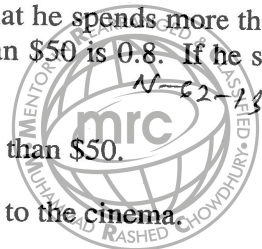


# Probability

2 On Saturday afternoons Mohit goes shopping with probability 0.25, or goes to the cinema with probability 0.35 or stays at home. If he goes shopping the probability that he spends more than \$50 is 0.7. If he goes to the cinema the probability that he spends more than \$50 is 0.8. If he stays at home he spends \$10 on a pizza.

(i) Find the probability that Mohit will go to the cinema and spend less than \$50. [1]

(ii) Given that he spends less than \$50, find the probability that he went to the cinema. [4]



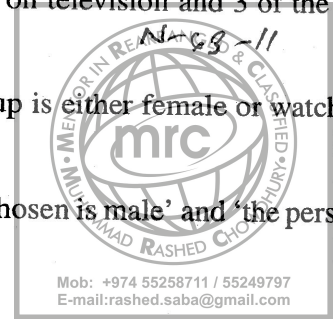
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# Probability

- 2 In a group of 30 teenagers, 13 of the 18 males watch 'Kops are Kids' on television and 3 of the 12 females watch 'Kops are Kids'.
- (i) Find the probability that a person chosen at random from the group is either female or watches 'Kops are Kids' or both. [4]
- (ii) Showing your working, determine whether the events 'the person chosen is male' and 'the person chosen watches Kops are Kids' are independent or not. [2]



# Probability

4 Tim throws a fair die twice and notes the number on each throw.

(i) Tim calculates his final score as follows. If the number on the second throw is a 5 he multiplies the two numbers together, and if the number on the second throw is not a 5 he adds the two numbers together. Find the probability that his final score is

(a) 12,

(b) 5.

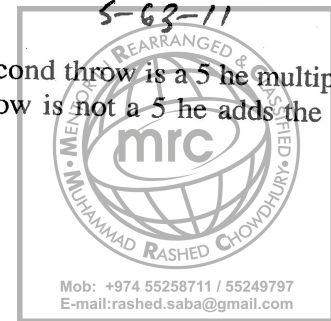
(ii) Events  $A$ ,  $B$ ,  $C$  are defined as follows.

$A$ : the number on the second throw is 5

$B$ : the sum of the numbers is 6

$C$ : the product of the numbers is even

By calculation find which pairs, if any, of the events  $A$ ,  $B$  and  $C$  are independent.



# Probability

- 2 When Joanna cooks, the probability that the meal is served on time is  $\frac{1}{5}$ . The probability that the kitchen is left in a mess is  $\frac{3}{5}$ . The probability that the meal is not served on time and the kitchen is not left in a mess is  $\frac{3}{10}$ . Some of this information is shown in the following table.

	Kitchen left in a mess	Kitchen not left in a mess	Total
Meal served on time			$\frac{1}{5}$
Meal not served on time		$\frac{3}{10}$	
Total			1

(i) Copy and complete the table.

[3]

(ii) Given that the kitchen is left in a mess, find the probability that the meal is not served on time.

[2]



# Probability

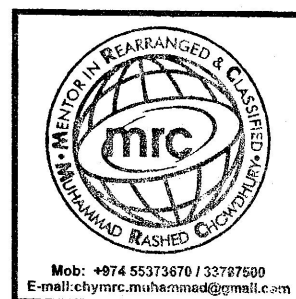
- 1 In a group of 30 adults, 25 are right-handed and 8 wear spectacles. The number who are right-handed and do not wear spectacles is 19.

- (i) Copy and complete the following table to show the number of adults in each category. [2]

	Wears spectacles	Does not wear spectacles	Total
Right-handed			
Not right-handed			
<b>Total</b>			<b>30</b>

An adult is chosen at random from the group. Event  $X$  is 'the adult chosen is right-handed'; event  $Y$  is 'the adult chosen wears spectacles'.

- (ii) Determine whether  $X$  and  $Y$  are independent events, justifying your answer. [3]





# Probability

- 5 Suzanne has 20 pairs of shoes, some of which have designer labels. She has 6 pairs of high-heeled shoes, of which 2 pairs have designer labels. She has 4 pairs of low-heeled shoes, of which 1 pair has designer labels. The rest of her shoes are pairs of sports shoes. Suzanne has 8 pairs of shoes with designer labels in total.

- (i) Copy and complete the table below to show the number of pairs in each category. [2]

	Designer labels	No designer labels	Total
High-heeled shoes			
Low-heeled shoes			
Sports shoes			
Total			20

Suzanne chooses 1 pair of shoes at random to wear.

- (ii) Find the probability that she wears the pair of low-heeled shoes with designer labels. [1]
- (iii) Find the probability that she wears a pair of sports shoes. [1]
- (iv) Find the probability that she wears a pair of high-heeled shoes, given that she wears a pair of shoes with designer labels. [1]
- (v) State with a reason whether the events 'Suzanne wears a pair of shoes with designer labels' and 'Suzanne wears a pair of sports shoes' are independent. [2]

Suzanne chooses 1 pair of shoes at random each day.

- (vi) Find the probability that Suzanne wears a pair of shoes with designer labels on at most 4 days out of the next 7 days. [3]



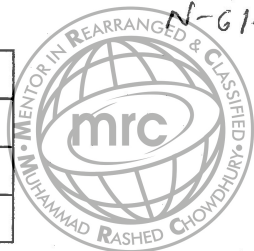


# Probability

- 2 The people living in two towns, Mumbok and Bagville, are classified by age. The numbers in thousands living in each town are shown in the table below.

	Mumbok	Bagville
Under 18 years	15	35
18 to 60 years	55	95
Over 60 years	20	30

One of the towns is chosen. The probability of choosing Mumbok is 0.6 and the probability of choosing Bagville is 0.4. Then a person is chosen at random from that town. Given that the person chosen is between 18 and 60 years old, find the probability that the town chosen was Mumbok. [5]



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# Probability

- 3 Ronnie obtained data about the gross domestic product (GDP) and the birth rate for 170 countries. He classified each GDP and each birth rate as either 'low', 'medium' or 'high'. The table shows the number of countries in each category.

		Birth rate		
		Low	Medium	High
GDP	Low	3	5	45
	Medium	20	42	12
	High	35	8	0

One of these countries is chosen at random.

- (i) Find the probability that the country chosen has a medium GDP. N-63-12 [1]
- (ii) Find the probability that the country chosen has a low birth rate, given that it does not have a medium GDP. [2]
- (iii) State with a reason whether or not the events 'the country chosen has a high GDP' and 'the country chosen has a high birth rate' are exclusive. [2]

One country is chosen at random from those countries which have a medium GDP and then a different country is chosen at random from those which have a medium birth rate.

- (iv) Find the probability that both countries chosen have a medium GDP and a medium birth rate. [3]



# Probability

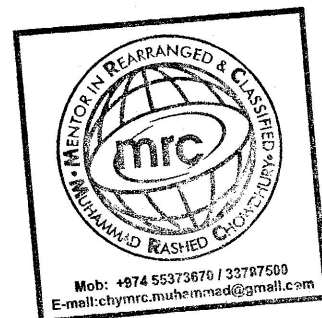
- 2 The faces of a biased die are numbered 1, 2, 3, 4, 5 and 6. The random variable  $X$  is the score when the die is thrown. The following is the probability distribution table for  $X$ .

$x$	1	2	3	4	5	6
$P(X = x)$	$p$	$p$	$p$	$p$	0.2	0.2

The die is thrown 3 times. Find the probability that the score is 4 on not more than 1 of the 3 throws.

[5]

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# Probability

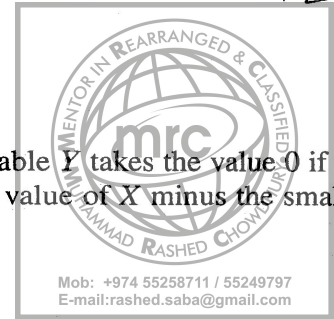
- 2 The random variable  $X$  has the probability distribution shown in the table.

$x$	2	4	6
$P(X = x)$	0.5	0.4	0.1

Two independent values of  $X$  are chosen at random. The random variable  $Y$  takes the value 0 if the two values of  $X$  are the same. Otherwise the value of  $Y$  is the larger value of  $X$  minus the smaller value of  $X$ .

- (i) Draw up the probability distribution table for  $Y$ .

- (ii) Find the expected value of  $Y$ .



# Probability

- 3 A spinner has 5 sides, numbered 1, 2, 3, 4 and 5. When the spinner is spun, the score is the number of the side on which it lands. The score is denoted by the random variable  $X$ , which has the probability distribution shown in the table.

$x$	1	2	3	4	5
$P(X = x)$	0.3	0.15	$3p$	$2p$	0.05

- (i) Find the value of  $p$ .

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[1]

A second spinner has 3 sides, numbered 1, 2 and 3. The score when this spinner is spun is denoted by the random variable  $Y$ . It is given that  $P(Y = 1) = 0.3$ ,  $P(Y = 2) = 0.5$  and  $P(Y = 3) = 0.2$ .

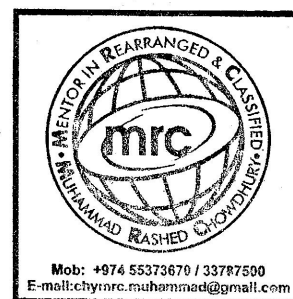
- (ii) Find the probability that, when both spinners are spun together,

(a) the sum of the scores is 4,

[3]

(b) the product of the scores is less than 8.

[3]





# Probability

7 James has a fair coin and a fair tetrahedral die with four faces numbered 1, 2, 3, 4. He tosses the coin once and the die twice. The random variable  $X$  is defined as follows.

- If the coin shows a **head** then  $X$  is the **sum** of the scores on the two throws of the die.
- If the coin shows a **tail** then  $X$  is the score on the **first throw** of the die only.

(i) Explain why  $X = 1$  can only be obtained by throwing a tail, and show that  $P(X = 1) = \frac{1}{8}$ . [2]

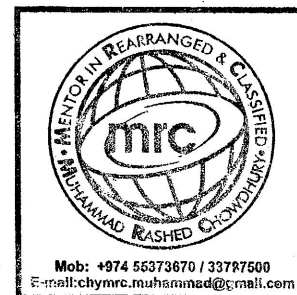
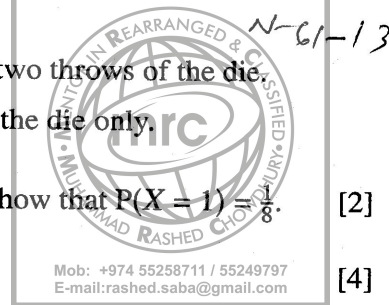
(ii) Show that  $P(X = 3) = \frac{3}{16}$ . [4]

(iii) Copy and complete the probability distribution table for  $X$ . [3]

$x$	1	2	3	4	5	6	7	8
$P(X = x)$	$\frac{1}{8}$		$\frac{3}{16}$		$\frac{1}{8}$		$\frac{1}{16}$	$\frac{1}{32}$

Event  $Q$  is 'James throws a tail'. Event  $R$  is 'the value of  $X$  is 7'.

(iv) Determine whether events  $Q$  and  $R$  are exclusive. Justify your answer. [2]

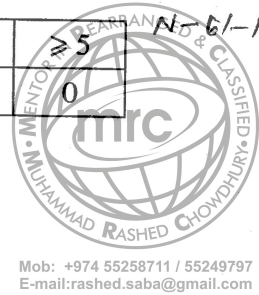


# Probability

- 2 The number of phone calls,  $X$ , received per day by Sarah has the following probability distribution.

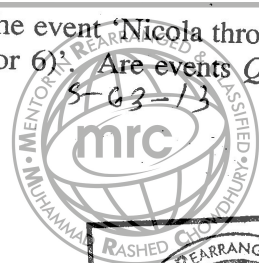
$x$	0	1	2	3	4	5
$P(X = x)$	0.24	0.35	$2k$	$k$	0.05	0

- (i) Find the value of  $k$ . [2]
- (ii) Find the mode of  $X$ . [1]
- (iii) Find the probability that the number of phone calls received by Sarah on any particular day is more than the mean number of phone calls received per day. [3]

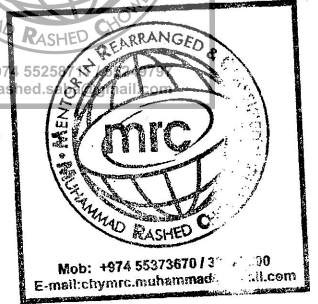


# Probability

- 1  $Q$  is the event 'Nicola throws two fair dice and gets a total of 5'.  $S$  is the event 'Nicola throws two fair dice and gets one low score (1, 2 or 3) and one high score (4, 5 or 6)'. Are events  $Q$  and  $S$  independent? Justify your answer. [4]



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# Probability

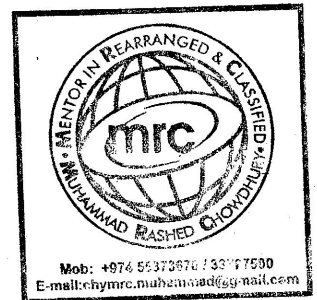
3 Jason throws two fair dice, each with faces numbered 1 to 6. Event  $A$  is 'one of the numbers obtained is divisible by 3 and the other number is not divisible by 3'. Event  $B$  is 'the product of the two numbers obtained is even'.

(i) Determine whether events  $A$  and  $B$  are independent, showing your working.

(ii) Are events  $A$  and  $B$  mutually exclusive? Justify your answer.



P  
[5]  
[1]

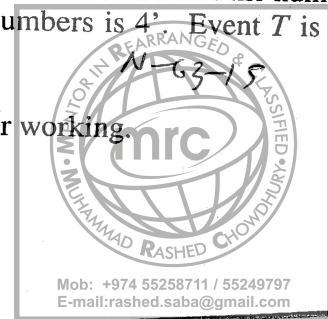


# Probability

3 Ellie throws two fair tetrahedral dice, each with faces numbered 1, 2, 3 and 4. She notes the numbers on the faces that the dice land on. Event  $S$  is 'the sum of the two numbers is 4'. Event  $T$  is 'the product of the two numbers is an odd number'.

(i) Determine whether events  $S$  and  $T$  are independent, showing your working. [5]

(ii) Are events  $S$  and  $T$  exclusive? Justify your answer. [1]





# Probability

- 5 Two fair twelve-sided dice with sides marked 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 are thrown, and the numbers on the sides which land face down are noted. Events  $Q$  and  $R$  are defined as follows.

$Q$  : the product of the two numbers is 24.

$R$  : both of the numbers are greater than 8.

- (i) Find  $P(Q)$ .
- (ii) Find  $P(R)$ .
- (iii) Are events  $Q$  and  $R$  exclusive? Justify your answer.
- (iv) Are events  $Q$  and  $R$  independent? Justify your answer.



[2]

[2]

[2]

[2]



# Probability

1 In a group of 30 adults, 25 are right-handed and 8 wear spectacles. The number who are right-handed and do not wear spectacles is 19.

(i) Copy and complete the following table to show the number of adults in each category. [2]

	Wears spectacles	Does not wear spectacles	Total
Right-handed			
Not right-handed			
Total			30

An adult is chosen at random from the group. Event  $X$  is 'the adult chosen is right-handed'; event  $Y$  is 'the adult chosen wears spectacles'.

(ii) Determine whether  $X$  and  $Y$  are independent events, justifying your answer. [3]



# Probability

- 4 For a group of 250 cars the numbers, classified by colour and country of manufacture, are shown in the table.

	Germany	Japan	Korea
Silver	40	26	34
White	32	22	26
Red	28	12	30

One car is selected at random from this group. Find the probability that the selected car is

(i) a red or silver car manufactured in Korea,

[1]

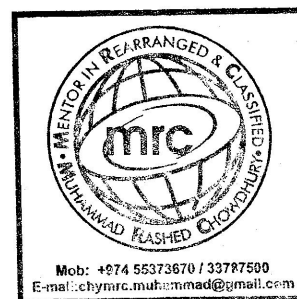
(ii) not manufactured in Japan.

[1]

$X$  is the event that the selected car is white.  $Y$  is the event that the selected car is manufactured in Germany.

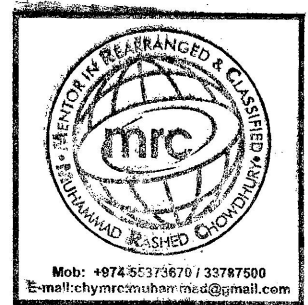
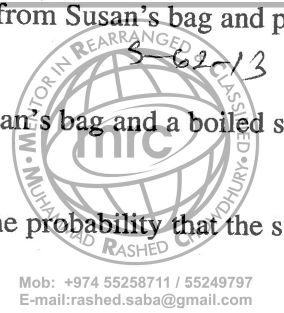
(iii) By using appropriate probabilities, determine whether events  $X$  and  $Y$  are independent.

[5]



# Probability

- 7 Susan has a bag of sweets containing 7 chocolates and 5 toffees. Ahmad has a bag of sweets containing 3 chocolates, 4 toffees and 2 boiled sweets. A sweet is taken at random from Susan's bag and put in Ahmad's bag. A sweet is then taken at random from Ahmad's bag.
- (i) Find the probability that the two sweets taken are a toffee from Susan's bag and a boiled sweet from Ahmad's bag. [2]
- (ii) Given that the sweet taken from Ahmad's bag is a chocolate, find the probability that the sweet taken from Susan's bag was also a chocolate. [4]
- (iii) The random variable  $X$  is the number of times a chocolate is taken. State the possible values of  $X$  and draw up a table to show the probability distribution of  $X$ . [5]



# Probability

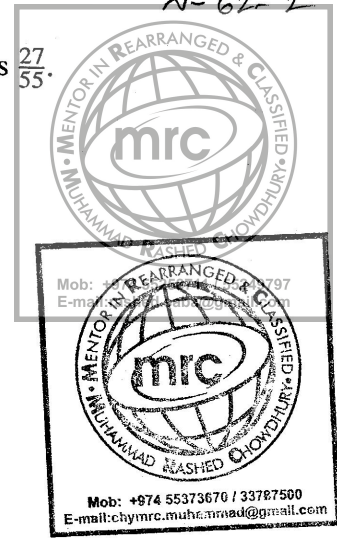
2. Noor has 3 T-shirts, 4 blouses and 5 jumpers. She chooses 3 items at random. The random variable  $X$  is the number of T-shirts chosen.

(i) Show that the probability that Noor chooses exactly one T-shirt is  $\frac{27}{55}$ .

[3]

(ii) Draw up the probability distribution table for  $X$ .

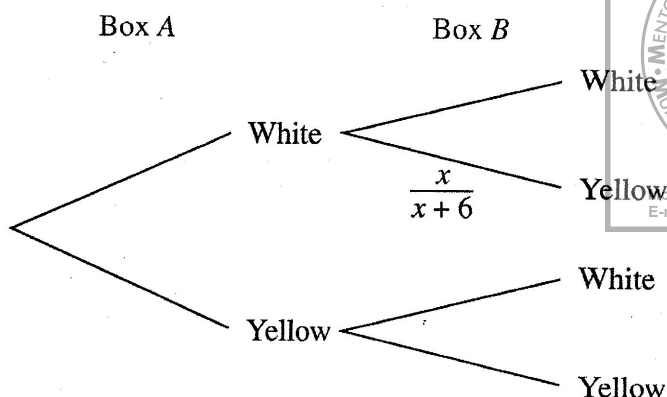
[4]





# Probability

- 7 Box A contains 8 white balls and 2 yellow balls. Box B contains 5 white balls and  $x$  yellow balls. A ball is chosen at random from box A and placed in box B. A ball is then chosen at random from box B. The tree diagram below shows the possibilities for the colours of the balls chosen.



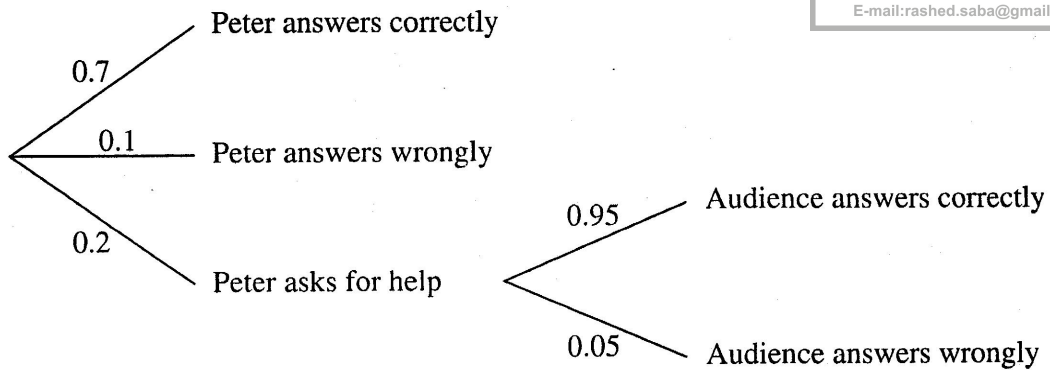
- (i) Justify the probability  $\frac{x}{x+6}$  on the tree diagram. [1]
- (ii) Copy and complete the tree diagram. [4]
- (iii) If the ball chosen from box A is white then the probability that the ball chosen from box B is also white is  $\frac{1}{3}$ . Show that the value of  $x$  is 12. [2]
- (iv) Given that the ball chosen from box B is yellow, find the conditional probability that the ball chosen from box A was yellow. [4]

# Probability

7 In a television quiz show Peter answers questions one after another, stopping as soon as a question is answered wrongly.

- The probability that Peter gives the correct answer himself to any question is 0.7.
- The probability that Peter gives a wrong answer himself to any question is 0.1.
- The probability that Peter decides to ask for help for any question is 0.2.

On the first occasion that Peter decides to ask for help he asks the audience. The probability that the audience gives the correct answer to any question is 0.95. This information is shown in the tree diagram below.



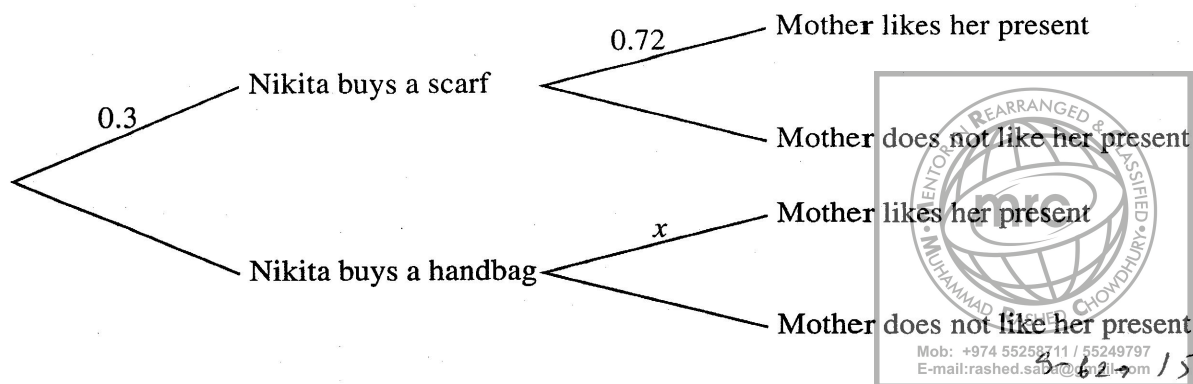
(i) Show that the probability that the first question is answered correctly is 0.89. [1]

On the second occasion that Peter decides to ask for help he phones a friend. The probability that his friend gives the correct answer to any question is 0.65.

- (ii) Find the probability that the first two questions are both answered correctly. [6]
- (iii) Given that the first two questions were both answered correctly, find the probability that Peter asked the audience. [3]

# Probability

4

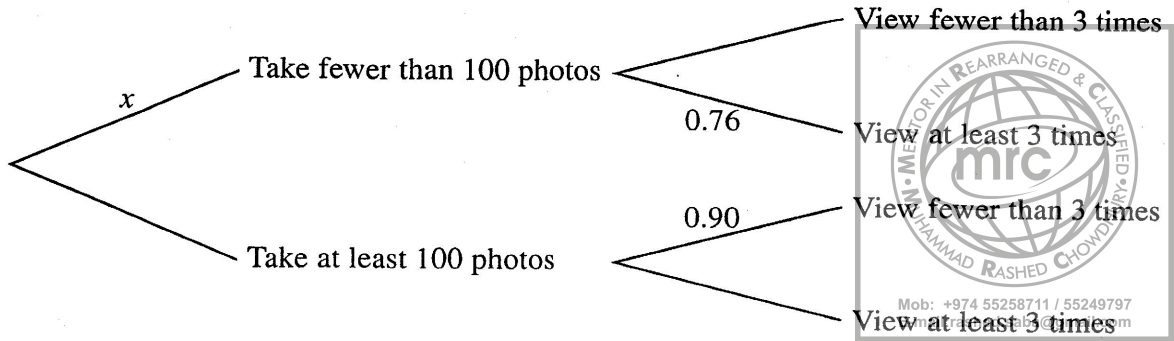


Nikita goes shopping to buy a birthday present for her mother. She buys either a scarf, with probability 0.3, or a handbag. The probability that her mother will like the choice of scarf is 0.72. The probability that her mother will like the choice of handbag is  $x$ . This information is shown on the tree diagram. The probability that Nikita's mother likes the present that Nikita buys is 0.783.

- (i) Find  $x$ . [3]
- (ii) Given that Nikita's mother does not like her present, find the probability that the present is a scarf. [4]

# Probability

4



A survey is undertaken to investigate how many photos people take on a one-week holiday and also how many times they view past photos. For a randomly chosen person, the probability of taking fewer than 100 photos is  $x$ . The probability that these people view past photos at least 3 times is 0.76. For those who take at least 100 photos, the probability that they view past photos fewer than 3 times is 0.90. This information is shown in the tree diagram. The probability that a randomly chosen person views past photos fewer than 3 times is 0.801.

S-6-15

(i) Find  $x$ .

[3]

(ii) Given that a person views past photos at least 3 times, find the probability that this person takes at least 100 photos.

[4]

# Probability

7 (a) (i) Find the probability of getting at least one 3 when 9 fair dice are thrown.  $S-61-11$  [2]

(ii) When  $n$  fair dice are thrown, the probability of getting at least one 3 is greater than 0.9. Find the smallest possible value of  $n$ . [4]

(b) A bag contains 5 green balls and 3 yellow balls. Ronnie and Julie play a game in which they take turns to draw a ball from the bag at random without replacement. The winner of the game is the first person to draw a yellow ball. Julie draws the first ball. Find the probability that Ronnie wins the game. [4]

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# Probability

3 It was found that 68% of the passengers on a train used a cell phone during their train journey. Of those using a cell phone, 70% were under 30 years old, 25% were between 30 and 65 years old and the rest were over 65 years old. Of those not using a cell phone, 26% were under 30 years old and 64% were over 65 years old.

- (i) Draw a tree diagram to represent this information, giving all probabilities as decimals. [2]
- (ii) Given that one of the passengers is 45 years old, find the probability of this passenger using a cell phone during the journey. [3]

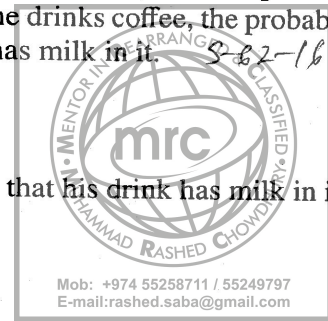
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# Probability

- 1 Ayman's breakfast drink is tea, coffee or hot chocolate with probabilities 0.65, 0.28, 0.07 respectively. When he drinks tea, the probability that he has milk in it is 0.8. When he drinks coffee, the probability that he has milk in it is 0.5. When he drinks hot chocolate he always has milk in it. S-82-16 Tr

(i) Draw a fully labelled tree diagram to represent this information. [2]

(ii) Find the probability that Ayman's breakfast drink is coffee, given that his drink has milk in it. [3]



# Probability

4 Sharik attempts a multiple choice revision question on-line. There are 3 suggested answers, one of which is correct. When Sharik chooses an answer the computer indicates whether the answer is right or wrong. Sharik first chooses one of the three suggested answers at random. If this answer is wrong he has a second try, choosing an answer at random from the remaining 2. If this answer is also wrong Sharik then chooses the remaining answer, which must be correct.

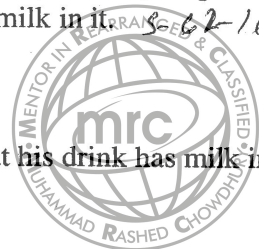
- (i) Draw a fully labelled tree diagram to illustrate the various choices that Sharik can make until the computer indicates that he has answered the question correctly. [4]
- (ii) The random variable  $X$  is the number of attempts that Sharik makes up to and including the one that the computer indicates is correct. Draw up the probability distribution table for  $X$  and find  $E(X)$ . [4]

# Probability

1 Ayman's breakfast drink is tea, coffee or hot chocolate with probabilities 0.65, 0.28, 0.07 respectively. <sup>74</sup> When he drinks tea, the probability that he has milk in it is 0.8. When he drinks coffee, the probability that he has milk in it is 0.5. When he drinks hot chocolate he always has milk in it. <sup>8-62-16</sup>

(i) Draw a fully labelled tree diagram to represent this information. [2]

(ii) Find the probability that Ayman's breakfast drink is coffee, given that his drink has milk in it. [3]



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# Probability

- 6 Nadia is very forgetful. Every time she logs in to her online bank she only has a 40% chance of remembering her password correctly. She is allowed 3 unsuccessful attempts on any one day and then the bank will not let her try again until the next day.

(i) Draw a fully labelled tree diagram to illustrate this situation. [3]

- (ii) Let  $X$  be the number of unsuccessful attempts Nadia makes on any day that she tries to log in to her bank. Copy and complete the following table to show the probability distribution of  $X$ . [4]

$x$	0	1	2	3
$P(X = x)$		0.24		

- (iii) Calculate the expected number of unsuccessful attempts made by Nadia on any day that she tries to log in. [2]