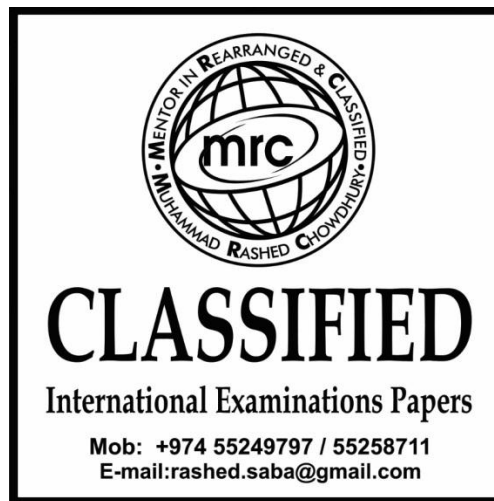



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## PURE MATHEMATICS 2/P2

TOPIC- Sequences and series

Sub-topic: **BINOMIAL EXPANSION**



*I Care Your Dream*

*mathematics is spicy*

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# THE BINOMIAL EXPANSION-05



10. The first 3 terms, in ascending powers of  $x$ , in the binomial expansion of  $(1 + ax)^{20}$  are given by

$$1 + 4x + px^2$$

where  $a$  and  $p$  are constants.

(a) Find the value of  $a$ .

(2)

(b) Find the value of  $p$ .

(2)

One of the terms in the binomial expansion of  $(1 + ax)^{20}$  is  $qx^4$ , where  $q$  is a constant.

(c) Find the value of  $q$ .

(2)

JA-17-I-12-10

# THE BINOMIAL EXPANSION-05



1. Find the first 4 terms, in ascending powers of  $x$ , of the binomial expansion of

$$\left(3 - \frac{1}{3}x\right)^5$$

giving each term in its simplest form.

(4)

JU-17

# THE BINOMIAL EXPANSION-05



5. (a) Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(2 - 9x)^4$$

giving each term in its simplest form.

(4)

$$f(x) = (1 + kx)(2 - 9x)^4, \text{ where } k \text{ is a constant}$$

The expansion, in ascending powers of  $x$ , of  $f(x)$  up to and including the term in  $x^2$  is

$$A - 232x + Bx^2$$

where  $A$  and  $B$  are constants.

- (b) Write down the value of  $A$ .

(1)

- (c) Find the value of  $k$ .

(2)

- (d) Hence find the value of  $B$ .

(2)

JU-16

# THE BINOMIAL EXPANSION-05



7. (a) Find the first 4 terms, in ascending powers of  $x$ , of the binomial expansion of  $(1 + kx)^8$ , where  $k$  is a non-zero constant. Give each term in its simplest form.

Given that the coefficient of  $x^3$  in this expansion is 1512

- (b) find the value of  $k$ .

JA-16-IAL-12

# THE BINOMIAL EXPANSION-05



1. The first three terms in ascending powers of  $x$  in the binomial expansion of  $(1 + px)^8$  are given by

$$1 + 12x + qx^2$$

where  $p$  and  $q$  are constants.

Find the value of  $p$  and the value of  $q$ .

(5)

JU-16-IAL-12

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$\left(2 - \frac{x}{4}\right)^{10}$$

giving each term in its simplest form.

(4)

JU-2015

# THE BINOMIAL EXPANSION-05



4. (a) Find the first 4 terms in ascending powers of  $x$  of the binomial expansion of

$$\left(2 + \frac{x}{4}\right)^{10}$$

giving each term in its simplest form.

**(4)**

- (b) Use your expansion to find an estimated value for  $2.025^{10}$ , stating the value of  $x$  which you have used and showing your working.

**(3)**

JA-2015



# THE BINOMIAL EXPANSION-05



6. (a) Find the first 3 terms in ascending powers of  $x$  of the binomial expansion of

$$(2 + ax)^6$$

where  $a$  is a non-zero constant. Give each term in its simplest form.

(4)

Given that, in the expansion, the coefficient of  $x$  is equal to the coefficient of  $x^2$

- (b) find the value of  $a$ .

(2)

JU-15-I-12

# THE BINOMIAL EXPANSION-05



4. (a) Find the first 4 terms in ascending powers of  $x$  of the binomial expansion of

$$\left(2 + \frac{x}{4}\right)^{10}$$

giving each term in its simplest form.

(4)

- (b) Use your expansion to find an estimated value for  $2.025^{10}$ , stating the value of  $x$  which you have used and showing your working.

(3)

JA-15-I-12

# THE BINOMIAL EXPANSION-05



3. (a) Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(2 - 3x)^6$$

giving each term in its simplest form.

(4)

- (b) Hence, or otherwise, find the first 3 terms, in ascending powers of  $x$ , of the expansion of

$$\left(1 + \frac{x}{2}\right)(2 - 3x)^6$$

(3)

JU-14

# THE BINOMIAL EXPANSION-05



1. The first three terms in ascending powers of  $x$  in the binomial expansion of  $(1 + px)^{12}$  are given by

$$1 + 18x + qx^2$$

where  $p$  and  $q$  are constants.

Find the value of  $p$  and the value of  $q$ .

(5)

JA-14

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms in ascending powers of  $x$  of

$$\left(2 - \frac{x}{2}\right)^6$$

giving each term in its simplest form.

(4)

JA-14-I-12

# THE BINOMIAL EXPANSION-05



2. (a) Use the binomial theorem to find all the terms of the expansion of

$$(2 + 3x)^4$$

Give each term in its simplest form.

(4)

- (b) Write down the expansion of

$$(2 - 3x)^4$$

in ascending powers of  $x$ , giving each term in its simplest form.

(1)

JU-2013

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms, in ascending powers of  $x$ , in the binomial expansion of

$$(2 - 5x)^6$$

Give each term in its simplest form.

(4)

JA-2013

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(2 - 3x)^5$$

giving each term in its simplest form.

**(4)**

JU-12



# THE BINOMIAL EXPANSION-05



3. (a) Find the first 4 terms of the binomial expansion, in ascending powers of  $x$ , of

$$\left(1 + \frac{x}{4}\right)^8$$

giving each term in its simplest form.

**(4)**

- (b) Use your expansion to estimate the value of  $(1.025)^8$ , giving your answer to 4 decimal places.

**(3)**

JA-12

## THE BINOMIAL EXPANSION-05



2. (a) Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(3 + bx)^5$$

where  $b$  is a non-zero constant. Give each term in its simplest form.

(4)

Given that, in this expansion, the coefficient of  $x^2$  is twice the coefficient of  $x$ ,

- (b) find the value of  $b$ .

(2)

JU-11

# THE BINOMIAL EXPANSION-05



5. Given that  $\binom{40}{4} = \frac{40!}{4!b!}$ ,

(a) write down the value of  $b$ .

**(1)**

In the binomial expansion of  $(1+x)^{40}$ , the coefficients of  $x^4$  and  $x^5$  are  $p$  and  $q$  respectively.

(b) Find the value of  $\frac{q}{p}$ .

**(3)**

JA-11

## THE BINOMIAL EXPANSION-05



4. (a) Find the first 4 terms, in ascending powers of  $x$ , of the binomial expansion of  $(1 + ax)^7$ , where  $a$  is a constant. Give each term in its simplest form.

(4)

Given that the coefficient of  $x^2$  in this expansion is 525,

- (b) find the possible values of  $a$ .

(2)

JU-10

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(3 - x)^6$$

and simplify each term.

(4)

JA-10

## THE BINOMIAL EXPANSION-05



2. (a) Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(2 + kx)^7$$

where  $k$  is a constant. Give each term in its simplest form.

(4)

Given that the coefficient of  $x^2$  is 6 times the coefficient of  $x$ ,

- (b) find the value of  $k$ .

(2)

JU-09

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of  $(3 - 2x)^5$ , giving each term in its simplest form.

(4)

JA-9

## THE BINOMIAL EXPANSION-05



3. (a) Find the first 4 terms, in ascending powers of  $x$ , of the binomial expansion of  $(1 + ax)^{10}$ , where  $a$  is a non-zero constant. Give each term in its simplest form.

(4)

Given that, in this expansion, the coefficient of  $x^3$  is double the coefficient of  $x^2$ ,

- (b) find the value of  $a$ .

(2)

JU-08



# THE BINOMIAL EXPANSION-05



3. (a) Find the first 4 terms of the expansion of  $\left(1 + \frac{x}{2}\right)^{10}$  in ascending powers of  $x$ , giving each term in its simplest form.

(4)

(b) Use your expansion to estimate the value of  $(1.005)^{10}$ , giving your answer to 5 decimal places.

(3)

JA-08

# THE BINOMIAL EXPANSION-05



3. (a) Find the first four terms, in ascending powers of  $x$ , in the binomial expansion of  $(1+kx)^6$ , where  $k$  is a non-zero constant.

(3)

Given that, in this expansion, the coefficients of  $x$  and  $x^2$  are equal, find

- (b) the value of  $k$ ,

(2)

- (c) the coefficient of  $x^3$ .

(1)

JU-7

## THE BINOMIAL EXPANSION-05



2. (a) Find the first 4 terms, in ascending powers of  $x$ , of the binomial expansion of  $(1-2x)^5$ . Give each term in its simplest form.

(4)

- (b) If  $x$  is small, so that  $x^2$  and higher powers can be ignored, show that

$$(1+x)(1-2x)^5 \approx 1-9x.$$

(2)

JA-7

# THE BINOMIAL EXPANSION-05



1. Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of  $(2 + x)^6$ , giving each term in its simplest form.

(4)

JU-06

# THE BINOMIAL EXPANSION-05



2. (a) Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(1 + px)^9,$$

where  $p$  is a constant.

(2)

The first 3 terms are 1,  $36x$  and  $qx^2$ , where  $q$  is a constant.

- (b) Find the value of  $p$  and the value of  $q$ .

(4)

JA-06

# THE BINOMIAL EXPANSION-05



4. (a) Write down the first three terms, in ascending powers of  $x$ , of the binomial expansion of  $(1 + px)^{12}$ , where  $p$  is a non-zero constant.

(2)

Given that, in the expansion of  $(1 + px)^{12}$ , the coefficient of  $x$  is  $(-q)$  and the coefficient of  $x^2$  is  $11q$ ,

- (b) find the value of  $p$  and the value of  $q$ .

(4)

JU-05