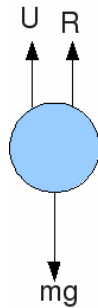
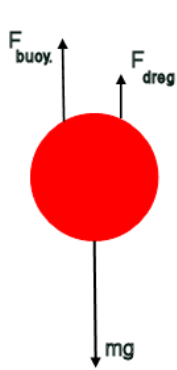


Mathematical Problems CH-07 part (I)



$$F + U = W$$

$$6\pi\eta r v + \rho_f \frac{4}{3}\pi r^3 g = \rho_b \frac{4}{3}\pi r^3 g$$

$$\eta = \frac{2r^2(\rho - \sigma)g}{9v} \quad \eta = \frac{2r^2\rho g}{9v} \quad v = \frac{2r^2(\rho - \sigma)g}{9\eta}$$

Q. An iron ball of radius 2×10^{-4} m is falling through tarpin oil at terminal velocity of 4×10^{-2} ms⁻¹. The densities of iron and tarpin oil are respectively 7.8×10^3 kg m⁻³ and 0.87×10^3 kg m⁻³. Calculate the co-efficient of viscosity of tarpin oil. [1.5×10^{-2} Nsm⁻²]

Q. A drop of water is falling through air. The terminal velocity of the drop is 1.2×10^{-2} ms⁻² and co-efficient of viscosity of air = 1.8×10^{-5} Nsm⁻². What is the diameter of the drop ? [Density of air = 1.21 kgm⁻³] [1.99×10^{-5} m]

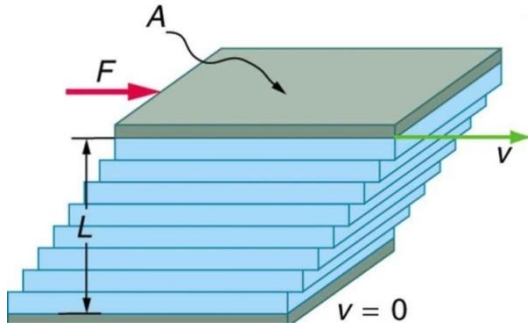
Q. Determine the radius of a drop of water falling through air with terminal velocity 1.2 cm s^{-1} .
The co-efficient of viscosity of air = $1.8 \times 10^{-5} \text{ N s m}^{-2}$ and density of air = 1.21 kg m^{-3} .

Q. Calculate the terminal velocity of a rain drop of diameter 0.03 mm . The co-efficient of viscosity of air is $1.8 \times 10^{-5} \text{ N s m}^{-2}$ and its density is 1.2 kg m^{-3} . [Ans. 2.7 cm s^{-1}]

Q. A spherical ball of radius $4 \times 10^{-4} \text{ m}$ is falling through glycerin at terminal velocity of $6.5 \times 10^{-3} \text{ ms}^{-1}$. The densities of material of the spherical ball and glycerin are respectively $11.37 \times 10^3 \text{ kg m}^{-3}$ and $1.26 \times 10^3 \text{ kg m}^{-3}$. Calculate the co-efficient of viscosity of glycerine. [Ans. 0.54 N s m^{-2}]

Q. Calculate the terminal velocity of a rain drop of radius 0.01 mm. The co-efficient of viscosity of air is $1.8 \times 10^{-5} \text{ N-sm}^{-2}$ and its density is 1.2 kgm^{-3} . Density of water = $1 \times 10^3 \text{ kgm}^{-3}$.

Q. An air bubble of diameter 2 mm steadily through a solution of density 1700 kg m^{-3} at the rate of 0.40 cm/s. Calculate the co-efficient of viscosity of the solution. The density of air is negligible.



$$F = -\eta A \frac{dv}{dx}$$

Q. A metal plate of area 100 cm^2 is placed on a layer of castor oil of thickness 0.2 cm . Calculate the horizontal force required to move the plate with a speed 3 cm s^{-1} . [Co-efficient of viscosity of oil = 1.55 N-sm^{-2}]

Q. A sheet of area 0.01 m^2 is placed on a layer of glycerin of 2 mm thickness. If a force of 0.4 N is required to move the sheet with velocity of 0.05 ms^{-1} . Calculate the co-efficient of viscosity. [1.6 N-sm^{-2}]

Q. A plate of area $10 \times 10^{-3} \text{ m}^2$ is placed on a layer of castor oil ($\eta = 1.55 \text{ N-sm}^{-2}$) of thickness $2 \times 10^{-3} \text{ m}$. Calculate the horizontal force required to move the plate with a speed of 0.05 ms^{-1} . [Ans. 0.3875 N]

Stokes' Law

$F = 6\pi\eta r v$

F = viscous drag (Newtons)
 η = viscosity of fluid (Pascal-seconds)
 r = radius (metres)
 v = velocity of object (m/s)

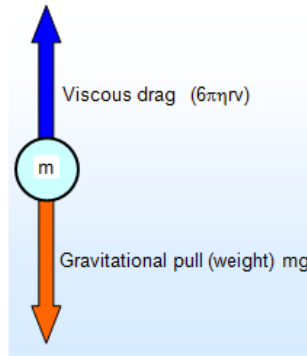


Figure 1

$$F = 6\pi\eta r v$$

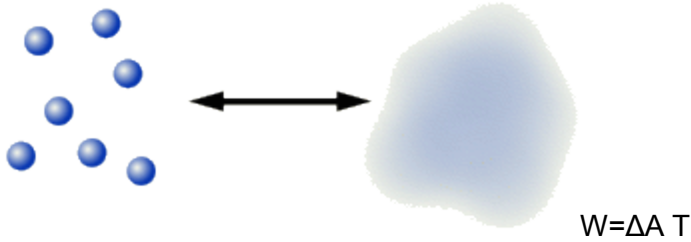
Q. A metal sphere of radius 200 mm is falling through a liquid with terminal velocity of $2.1 \times 10^{-2} \text{ ms}^{-1}$. The co-efficient of viscosity of the liquid 0.003 N-sm^{-2} . Calculate the viscous force of the liquid.

Q. A plate of area $10 \times 10^{-3} \text{ m}^2$ is placed on a layer of castor oil ($\eta = 1.55 \text{ N-sm}^{-2}$) of thickness $2 \times 10^{-3} \text{ m}$. Calculate the horizontal force required to move the plate with a speed of 0.05 ms^{-1} .
 [Ans. 0.3875 N]

Q. A sheet of area 2cm^2 is placed on a layer of glycerin of 3 mm thickness. If a force of 0.5 N is required to move the sheet with velocity of 4 cm s^{-1} , calculate the co-efficient of viscosity . [Ans. $1.875\text{N}\cdot\text{sm}^{-2}$]

Q. A metal sphere of radius 25 cm is falling through a liquid with terminal velocity of 2.5 cm s^{-1} . The co-efficient of viscosity of the liquid is $0.005\text{ N}\cdot\text{sm}^{-2}$. Calculate the viscous force of the liquid .
[Ans. $0.588 \times 10^{-4}\text{ N}$]

Q. Eight rain drops of radius 1mm each falling downwards with a terminal velocity of 6cm s^{-1} coalesces to form a bigger drop. Find the terminal velocity of the bigger drop. [24cm s^{-1}]



$$\Delta A = 2 \times 4\pi (r_2^2 - r_1^2)$$

Q. A large drop is formed by 25 small drops of water, each of diameter 0.17×10^{-2} m. Find the energy released. [Surface tension of water = $72 \times 10^{-3} \text{ Nm}^{-1}$]

Q. A water drop of radius 0.5 cm is broken into one million (10^6) equal droplets. Calculate the gain in surface energy and the applied energy. [Surface tension of water $72 \times 10^{-3} \text{ Nm}^{-1}$]

Q. A water drop of radius 10^{-2} m is broken into 1000 equal droplets. Calculate the gain in surface energy. [Surface tension of water = 0.075 Nm^{-1}] [Ans. $8.5 \times 10^{-4} \text{ J}$]

Q. A large drop is formed by 10^3 small drops of water each of radius 1 mm. Find the energy released. [Surface tension of water = $72 \times 10^{-3} \text{ Nm}^{-1}$] [Ans. $11.304 \times 10^{-5} \text{ J}$]

Q. A water drop of radius 10^{-4} m is broken into 125 equal droplets. Calculate the increase in surface energy. [Surface tension of water = $7.2 \times 10^{-2} \text{ Nm}^{-1}$] [Ans. $3.62 \times 10^{-8} \text{ J}$]



Q. A soap bubble of radius 2 cm. is slowly increased and it reaches to a bubble of radius 3cm.
[Surface tension of soap solution $4 \times 10^{-2} \text{ Nm}^{-1}$]

Q. Two mercury drops each of radius r merge to form a bigger drop. Calculate the surface energy released.
[Ans. $1.65 \pi r^2 T$]